

Algebra Mastery Test Practice 2 (2018)

All questions are worth 3 points.

Solve for the variable.

1) $7y + 5 - 3y = -31$

$$\begin{array}{r} 4y + 5 = -31 \\ -5 \quad | \quad -5 \\ \hline 4y = -36 \\ \div 4 \quad | \quad \div 4 \\ \hline y = -9 \end{array}$$

Answers

1) $y = -9$

2) $8(b + 7) = 32 + 2b$

$$\begin{array}{r} 8b + 56 = 32 + 2b \\ -2b \quad | \quad -2b \\ \hline 6b + 56 = 32 \\ -56 \quad | \quad -56 \\ \hline 6b = -24 \\ \div 6 \quad | \quad \div 6 \\ \hline b = -4 \end{array}$$

2) $b = -4$

3) $\frac{1}{3}(15n - 9) = 3n + 20$

$$\begin{array}{r} 5n - 3 = 3n + 20 \\ -3n \quad | \quad -3n \\ \hline 2n - 3 = 20 \\ +3 \quad | \quad +3 \\ \hline 2n = 23 \\ \div 2 \quad | \quad \div 2 \\ \hline n = 11.5 \end{array}$$

3) $n = 11.5$

4) $6(c - 5) - 3c = c + 10$

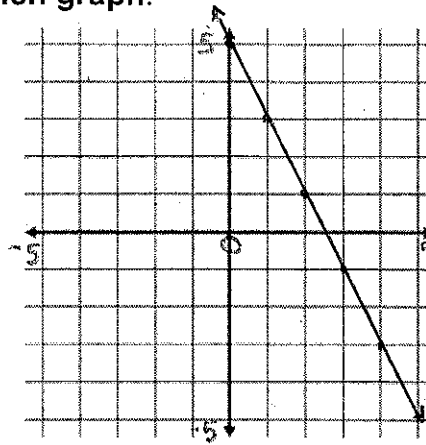
$$\begin{array}{r} 6c - 30 - 3c = c + 10 \\ 3c - 30 = c + 10 \\ -c \quad | \quad -c \\ \hline 2c - 30 = 10 \\ +30 \quad | \quad +30 \\ \hline 2c = 40 \\ \div 2 \quad | \quad \div 2 \\ \hline c = 20 \end{array}$$

4) $c = 20$

Model each rule with a table of values and then graph.

5) $y = -2x + 5$

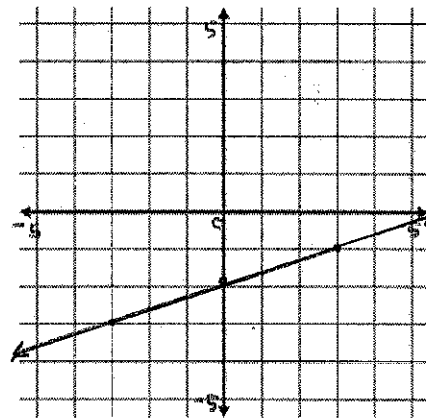
x	Rule: $y = -2x + 5$	y
-1	$-2(-1) + 5$	7
0	$-2(0) + 5$	5
1	$-2(1) + 5$	3
2	$-2(2) + 5$	1



5) see left

6) $y = \frac{1}{3}x - 2$

x	Rule: $y = \frac{1}{3}x - 2$	y
-1	$\frac{1}{3}(-1) - 2$	$-2\frac{1}{3}$
0	$\frac{1}{3}(0) - 2$	-2
1	$\frac{1}{3}(1) - 2$	$-1\frac{2}{3}$
2	$\frac{1}{3}(2) - 2$	$-1\frac{1}{3}$



6) see left

Find the function rule.

7)

x	Y
-3	10
-1	-3
1	4
3	11

$m = \frac{7}{2} = 3\frac{1}{2}$

$$y - y_1 = m(x - x_1)$$

$$y - 4 = 3\frac{1}{2}(x - 1)$$

$$y - 4 = 3\frac{1}{2}x - 3\frac{1}{2}$$

$$+4 \quad \quad \quad +4$$

$$y = 3\frac{1}{2}x + \frac{1}{2}$$

7) $y = 3\frac{1}{2}x + \frac{1}{2}$

8)

x	y
-1	$-2\frac{1}{4}$
1	-2
3	$-1\frac{3}{4}$
5	$-1\frac{1}{2}$

$m = \frac{1}{4} \div 2 = \frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$

$$y - y_1 = m(x - x_1)$$

$$y + 2 = \frac{1}{8}(x - 1)$$

$$y + 2 = \frac{1}{8}x - \frac{1}{8}$$

$$+2 \quad \quad \quad +2$$

$$y = \frac{1}{8}x - 2\frac{1}{8}$$

8) $y = \frac{1}{8}x - 2\frac{1}{8}$

9) Sarah has hired a go-kart track for her birthday. She paid a deposit of \$120 then will pay \$25 for each friend she invites. Write an equation and state how much Sarah will pay if a total of 8 people drive go-karts.

$$y = 25x + 120$$

$$y = 25(8) + 120$$

$$y = 200 + 120$$

$$y = \$320$$

9) \$320

10) While babysitting you are asked to fill a paddling pool. The pool has 5 gallons of water already. The hose fills the pool with 2 gallons of water every minute. Write an equation and state how much water will be in the pool after 4 minutes.

$$y = 2x + 5$$

$$y = 2(4) + 5$$

$$y = 8 + 5$$

$$y = 13 \text{ gallons}$$

10) 13 gal.

Write each equation in Standard Form using **integers.**

11) $2y = \frac{2}{3}x - 14$

$$\frac{-\frac{2}{3}x}{-\frac{2}{3}x} \mid \frac{-\frac{2}{3}x}{-\frac{2}{3}x}$$

$$-\frac{2}{3}x + 2y = -14$$

LCD = 3

$$3\left(-\frac{2}{3}x + 2y = -14\right)$$

$$-2x + 6y = -42$$

11) _____
 $-2x + 6y = -42$

12) $y = -\frac{1}{3}x + \frac{3}{4}$

$$\frac{+\frac{1}{3}x}{+\frac{1}{3}x} \mid \frac{+\frac{1}{3}x}{+\frac{1}{3}x}$$

$$\frac{1}{3}x + y = \frac{3}{4}$$

LCD = 12 (3x4)

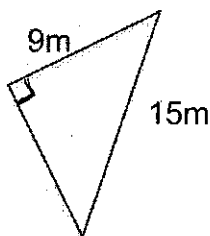
$$12\left(\frac{1}{3}x + y = \frac{3}{4}\right)$$

$$4x + 12y = 9$$

12) _____
 $4x + 12y = 9$

Use Pythagorean Theorem to solve for the missing length.

13)



$$a^2 + b^2 = c^2$$

$$9^2 + b^2 = 15^2$$

$$81 + b^2 = 225$$

$$\begin{array}{r} -81 \\ 81 + b^2 = 225 \\ \hline b^2 = 144 \end{array}$$

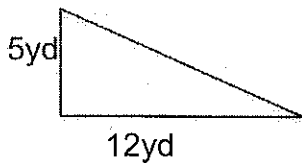
$$b^2 = 144$$

$$b = \sqrt{144} = 12m$$

13) 12m

Use Pythagorean Theorem to solve for the missing length.

14)



$$a^2 + b^2 = c^2$$

$$5^2 + 12^2 = c^2$$

$$25 + 144 = c^2$$

$$169 = c^2$$

$$c = 13 \text{yd}$$

14) 13yd

Graph the following systems of equations

15) $y = -2x + 6$
 $3x + 4y = 24$

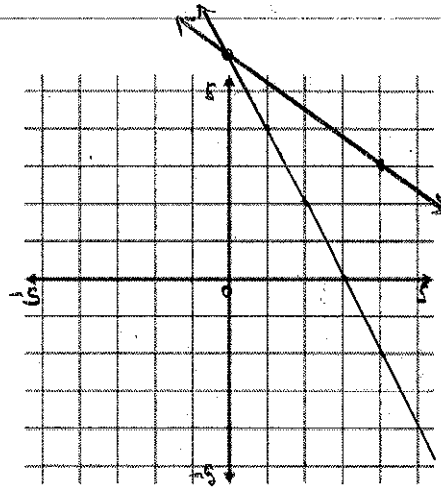
$$3x + 4y = 24$$

$$\underline{-3x} \quad \underline{12y} \quad \underline{-72}$$

$$4y = -3x + 24$$

$$\underline{4y} \quad \underline{12y} \quad \underline{4}$$

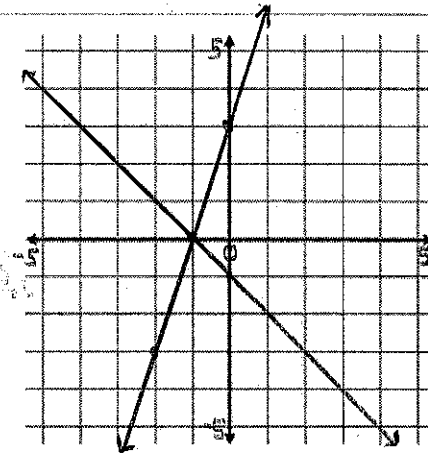
$$y = -\frac{3}{4}x + 6$$



15) (0, 6)

Graph the following systems of equations

$y = 3x + 3$
 $y = -x - 1$



16) (0, -1)

Solve each system of equations using substitution.

16) $3x - y = 4$
 $x + 5y = -4$
 $\underline{-5y} \quad \underline{-5y}$
 $x = -5y - 4$

$$3x - y = 4$$

$$3(-5y - 4) - y = 4$$

$$\boxed{-15y} \quad \boxed{-12} \quad \boxed{-y} = 4$$

$$\underline{-16y - 12 = 4}$$

$$\underline{+12} \quad \underline{+12}$$

$$\underline{-16y = 16}$$

$$\underline{\div -16} \quad \underline{\div -16}$$

$$y = -1$$

$$3x - y = 4$$

$$3x - (-1) = 4$$

$$3x = 3$$

$$\underline{\div 3} \quad \underline{\div 3}$$

$$x = 1$$

16) (1, -1)

Solve each system of equations using substitution.

17) $x + y = 4$
 $y = 7x + 4$

$$\begin{array}{r} x + y = 4 \\ x + (7x + 4) = 4 \\ 8x + 4 = 4 \\ -4 \quad | -4 \\ \hline 8x = 0 \\ \div 8 \quad | \div 8 \\ \hline x = 0 \end{array}$$

$$\begin{array}{l} y = 7x + 4 \\ y = 7(0) + 4 \\ y = 4 \end{array}$$

17) $(0, 4)$

Solve each system of equations using elimination

18) $x + y = 19$
 $x - y = -7$

$$\begin{array}{r} x + y = 19 \\ - \quad x - y = -7 \\ \hline 2y = 26 \\ \div 2 \quad | \div 2 \\ \hline y = 13 \end{array}$$

$$\begin{array}{r} x + y = 19 \\ x + 13 = 19 \\ -13 \quad | -13 \\ \hline x = 6 \end{array}$$

18) $(6, 13)$

19) $-3x + 4y = 29$
 $+3x + 2y = -17$

$$\begin{array}{r} 6y = 12 \\ \div 6 \quad | \div 6 \\ \hline y = 2 \end{array}$$

$$\begin{array}{r} -3x + 4y = 29 \\ -3x + 4(2) = 29 \\ -3x + 8 = 29 \\ -8 \quad | -8 \\ \hline -3x = 21 \\ \div -3 \quad | \div -3 \\ \hline x = -7 \end{array}$$

19) $(-7, 2)$

20) The school that Stefan goes to is selling tickets to a choral performance. On the first day of ticket sales the school sold 3 senior citizen tickets and 1 child ticket for a total of \$38. The school took in \$52 on the second day by selling 3 senior citizen tickets and 2 child tickets. Find the price of a senior citizen ticket and the price of a child ticket.

$$\begin{array}{r} 3x + 1y = 38 \\ - \quad 3x + 2y = 52 \\ \hline -y = -14 \\ y = \$14 \end{array}$$

$$\begin{array}{r} 3x + y = 38 \\ 3x + 14 = 38 \\ -14 \quad | -14 \\ \hline 3x = 24 \\ \div 3 \quad | \div 3 \\ \hline x = \$8 \end{array}$$

Senior Citizen tickets are \$8 and Child tickets are \$14.

20) $(8, 14)$

Simplify.

21) $\frac{4m^6n^4}{20m^4n}$

$$\frac{4}{20} \cdot \frac{m^6}{m^4} \cdot \frac{n^4}{n}$$
$$\frac{1}{5} \cdot \frac{m^2}{1} \cdot \frac{n^3}{1}$$

Answer: $\frac{m^2n^3}{5}$

22) $\frac{3ab^4d^3}{6a^4c}$

$$\frac{3}{6} \cdot \frac{a}{a^4} \cdot \frac{b^4}{1} \cdot \frac{1}{c} \cdot \frac{d^3}{1}$$
$$\frac{1}{2} \cdot \frac{1}{a^3} \cdot \frac{b^4}{1} \cdot \frac{1}{c} \cdot \frac{d^3}{1}$$

Answer: $\frac{b^4d^3}{2a^3c}$

Evaluate the expression. Write your answer in scientific notation. (2pts)

21) $(6.9 \times 10^{-5}) + (4.5 \times 10^{-4})$

$$0.69 \times 10^{-4}$$

$$\begin{array}{r} 0.69 \\ + 4.50 \\ \hline 5.19 \end{array}$$

Answer: 5.19×10^{-4}

22) $(5.5 \times 10^4) - (2.3 \times 10^3)$

$$0.23 \times 10^4$$

$$\begin{array}{r} 5.50 \\ - 0.23 \\ \hline 5.27 \end{array}$$

Answer: 5.27×10^4

23) $(2.4 \times 10^8) \times (1.4 \times 10^8)$

$$2.4 \times 1.4 \times 10^{(8+8)}$$

$$3.36 \times 10^{16}$$

Answer: 3.36×10^{16}

Evaluate the expression. Write your answer in scientific notation. (2pts)

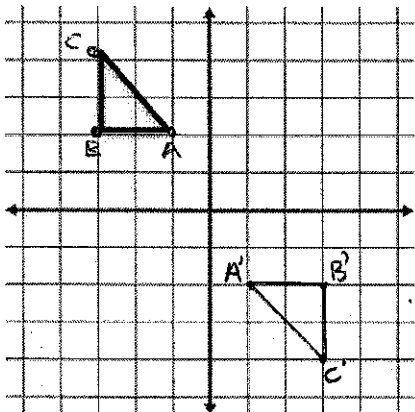
24) $(2.4 \times 10^0) \div (8 \times 10^2)$

$8 \overline{) 2.4}^{0.3}$ OR $3 \times 10^{-1} \times 10^{(0-2)}$
 3×10^{-3}

Answer: 3×10^3

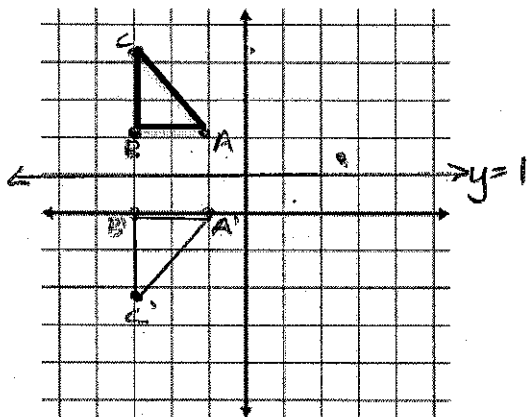
Rotate the triangle 180°.

23)



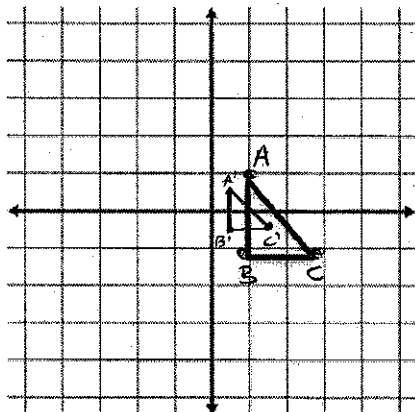
Reflect the triangle in the line $y = 1$.

24)



Draw the triangle with dilation 0.5 about the origin.

25)



$A(1, -1) \xrightarrow{\times 0.5} A'(\frac{1}{2}, -\frac{1}{2})$
 $B(1, -2) \rightarrow B'(\frac{1}{2}, -1)$
 $C(3, -2) \rightarrow C'(1\frac{1}{2}, -1)$